

Application and Effect Evaluation of Machine Learning in Mathematics Education Assessment and Feedback

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Abstract: The application of machine learning to assessment and feedback in mathematics education has received considerable attention in recent years. With the rapid advancement of artificial intelligence technologies, the integration of these innovations into educational assessments can significantly improve the accuracy and comprehensiveness of student learning assessments. This study examines how machine learning, specifically clustering algorithms such as Fuzzy C-Means (FCM), can be used to analyze student performance data to enable personalized and targeted instructional strategies. The complexity of educational research requires a multifaceted approach to evaluation, and the incorporation of fuzzy evaluation methods can address the inherent uncertainties in educational contexts. By exploring the historical evolution of educational assessment and utilizing advanced data analysis techniques, this research aims to provide insights into the development of more effective and nuanced assessment systems for mathematics education.

Keywords: Application, effect evaluation, machine learning, mathematics education, assessment and feedback

1. INTRODUCTION

In recent years, with the rapid development of artificial intelligence technology, how to effectively use these technologies to promote educational evaluation reform, help teachers fully understand and grasp the status of learners, and accurately evaluate the learning status based on the data generated by learners, and promote the improvement of learners' comprehensive ability and quality has become a hot issue in the education sector. Educational evaluation not only requires quantification of students' academic performance, but also requires a comprehensive evaluation of their comprehensive quality and ability, which is exactly the field where artificial intelligence technology has great potential. In educational evaluation, the concept of machine learning is also applicable. If a computer can check the effect of students' "learning", then it can "teach" students knowledge and evaluate students' knowledge mastery. In short, if a computer is trained to "learn" evaluation criteria, judge students' understanding and mastery of knowledge (whether written or oral), and match students' answers according to established standards, then it has the potential to be applied to educational evaluation. Through such a system, teachers can more efficiently obtain each student's learning progress and weak links, so as to provide targeted tutoring.

For educators, there is a difference between mastering knowledge and being able to understand and flexibly apply knowledge. Therefore, there is a difference between human judgment and machine judgment in educational assessment, and this difference is particularly evident in computer-based student writing assessment. Machines can judge students' writing level by analyzing a large number of writing samples, but it is difficult for them to understand the deep meaning and creative expression of the article like human evaluators. This requires integrating the advantages of artificial intelligence and human intelligence in the process of technology application to ensure the comprehensiveness and accuracy of the assessment. The application of artificial intelligence technology in educational assessment also involves the planning of personalized learning paths. Based on students'

learning data, artificial intelligence can tailor a learning plan for each student, recommend the most suitable learning resources and course content for them, and help them better master knowledge. This personalized learning plan not only improves learning efficiency, but also stimulates students' interest and initiative in learning. Artificial intelligence technology can also conduct in-depth analysis of students' learning behavior through big data analysis and natural language processing technology. For example, by analyzing students' click behavior, homework submission time, and class discussion participation on online learning platforms, students' academic performance and the possible learning difficulties can be predicted, so that intervention measures can be taken in advance to help students overcome the learning obstacles.

2. THE PROPOSED METHODOLOGY

2.1 The Complexity of Education and Fuzzy Evaluation

In the field of education, the complexity of the objects of educational research is particularly significant. When people are the subject and object of research, their thinking, emotions, will, and behavior not only have various characteristics of the natural material world, but also have subjective initiative. Their essence is a world of meaning and value that must be truly grasped through understanding. The world of education is not a purely factual world, but a cultural world. The core of the cultural world is value and meaning, which has strong individuality, diversity, acquisition, and contingency. The complexity of educational objects and educational systems will inevitably lead to a difficult development process for the discipline of education, and it will be challenged by other disciplines and research paradigms.

It is difficult for pedagogy to form a discipline system with a fixed research paradigm. The complexity of the educational system requires pedagogy to consider the relevant factors surrounding educational activities in discipline construction. Therefore, discipline construction must focus on correlation

analysis to establish the relationship between relevant factors in educational activities. Educational complexity research is guided by complexity thinking, and uses the principles and methods of complexity science to conduct educational research, which only adapts to the complex phenomenon of education itself. Understanding educational complexity helps us to clarify the ideas of educational research from a macro perspective and to guide educational evaluation. The complexity of education requires discipline construction: extracting unique research fields by using the research paradigms of other disciplines and determining the corresponding research objects. The development of modern education began after the industrial revolution and has the characteristics of production orders, which has led to the dismemberment and fragmentation of educational purposes, the pro-ceduralization of teaching processes, the mechanization of teaching behaviors, and the visualization of education and teaching evaluation. These phenomena can no longer meet the needs of education for the comprehensive development of human beings. In order to carry out all levels and types of educational work, develop education in the new era, and meet the characteristics of the complexity of education, we must introduce "fuzzy evaluation" when establishing an educational evaluation mechanism.

In actual educational evaluation, fuzzy evaluation methods can better cope with this complexity. By introducing fuzzy mathematics and fuzzy logic, fuzzy evaluation can deal with uncertainty and fuzziness, making the evaluation results more comprehensive and flexible. For example, in the evaluation of students' comprehensive quality, fuzzy evaluation can comprehensively consider students' performance in different aspects and evaluate them as a whole through a fuzzy comprehensive evaluation model. This method can not only reflect the true level of students, but also provide a scientific basis for educational decision-making. In addition, the complexity of educational evaluation also requires us to continuously innovate and improve evaluation standards and methods. For example, in teacher evaluation, in addition to the traditional teaching effect and student feedback, it is also necessary to consider factors such as teachers' professional development, educational research ability, and teaching innovation. Only by comprehensively using a variety of evaluation methods, such as combining quantitative evaluation with qualitative evaluation, and combining process evaluation with result evaluation, can the comprehensive quality and educational level of teachers be fully and accurately reflected.

2.2 The Application of Cluster Analysis Technology in Educational Evaluation

Partition clustering algorithm is an important method in cluster analysis. Compared with other algorithms, it has lower complexity, simple operation and efficient convergence speed. The core of this algorithm is to classify the data element set and classify the elements with high similarity into the same class. Each class contains at least one data element, and each data element can belong to only one class. Since student performance data has the characteristics of strong similarity and few noise points, it is suitable for analysis using partition clustering algorithm, among which the most typical algorithm is Fuzzy C-Means (FCM) algorithm. Expanding this content, we can further explore the application and improvement of partition clustering algorithm. FCM algorithm performs well in many practical problems, such as image processing, market segmentation, and medical diagnosis. Its basic idea is to minimize the sum of distances from each data point to each

cluster center by iteratively updating the cluster center and membership relationship matrix. The specific procedure is as follows: First, k cluster centers are randomly initialized; then, the distance from each data point to each cluster center is calculated according to the Euclidean distance, and the membership of each data point to each cluster is updated according to the fuzzy membership function. Then, calculate the new cluster center according to the updated membership. Repeat the above steps until the change in cluster center is less than the preset threshold or the maximum number of iterations is reached.

When analyzing student performance data, the FCM algorithm can effectively group students with similar performance into the same group, thereby identifying groups of students at different levels. This helps teachers develop more targeted lesson plans based on the characteristics of different groups of students and improve teaching effectiveness. In specific applications, the student performance data can be pre-processed, such as normalization, to eliminate the influence of different subject performance dimensions. Then, an appropriate number of clusters k are selected and the FCM algorithm is run to obtain the clustering results.

2.3 The Mathematics Education Assessment and Feedback

Mathematics education evaluation is an important branch of educational evaluation. By studying the history of educational evaluation and examining its development and changes from a longitudinal perspective, we can have a deeper understanding of the connotation and expansion of mathematics education evaluation. Combined with cluster analysis methods, the accuracy and scientificity of mathematics education evaluation can be further improved. Looking at the history of educational evaluation, various evaluation methods and theories have emerged over time. From traditional qualitative evaluation to modern quantitative evaluation and then to today's popular data-based evaluation methods, the development of these methods reflects the continuous progress of educational evaluation theory and practice. By examining these changes, it can be seen that mathematics education evaluation has undergone a transformation from simple performance assessment to complex multidimensional analysis. This transformation not only improves the accuracy of evaluation, but also promotes a comprehensive understanding of students' mathematical abilities.

The specific steps are as follows:

Data Collection and Preprocessing: First, collect student math performance data, including daily homework scores, test scores, class participation, etc. Preprocess these data, such as removing outliers and standardizing them, to ensure the quality and consistency of the data.

Determine the number of clusters: Select the appropriate number of clusters k according to your actual needs. The elbow method, silhouette coefficient method and other methods can be used to determine the optimal number of clusters.

Execute the clustering algorithm: Select an appropriate clustering algorithm, such as K-means algorithm or Fuzzy C-means (FCM) algorithm, perform cluster analysis, and divide students into different groups.

Analyze the results: Analyze the clustering results to understand the characteristics of students in different groups

in mathematics learning. For example, it may be found that students in one group perform well in geometry problems, while students in another group have difficulty in algebra problems.

Develop instructional strategies: Based on the results of cluster analysis, teachers can develop more targeted instructional strategies. For example, provide more challenging geometry problems for students who are strong in geometry, and provide more algebra practice and tutoring for students who are weak in algebra.

3. CONCLUSION

Incorporating machine learning into mathematics education assessment represents a transformative approach to understanding and improving student learning outcomes. This study highlights the potential of clustering algorithms, such as the Fuzzy C-Means (FCM) algorithm, to categorize students based on their performance data, facilitating the development of customized educational strategies. The complexity inherent in educational research requires robust and adaptable evaluation methods. Fuzzy evaluation, with its ability to handle ambiguity and provide comprehensive insights, complements the analytical capabilities of machine learning. By examining the historical evolution of educational evaluation methods, this research underscores the need for evaluation practices to evolve to keep pace with technological advances. The findings suggest that the integration of artificial intelligence into educational assessment not only improves the accuracy of assessments, but also empowers educators to tailor instruction to individual student needs, ultimately fostering a more effective and inclusive learning environment.

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